

# BEYOND POPULAR SCIENCE



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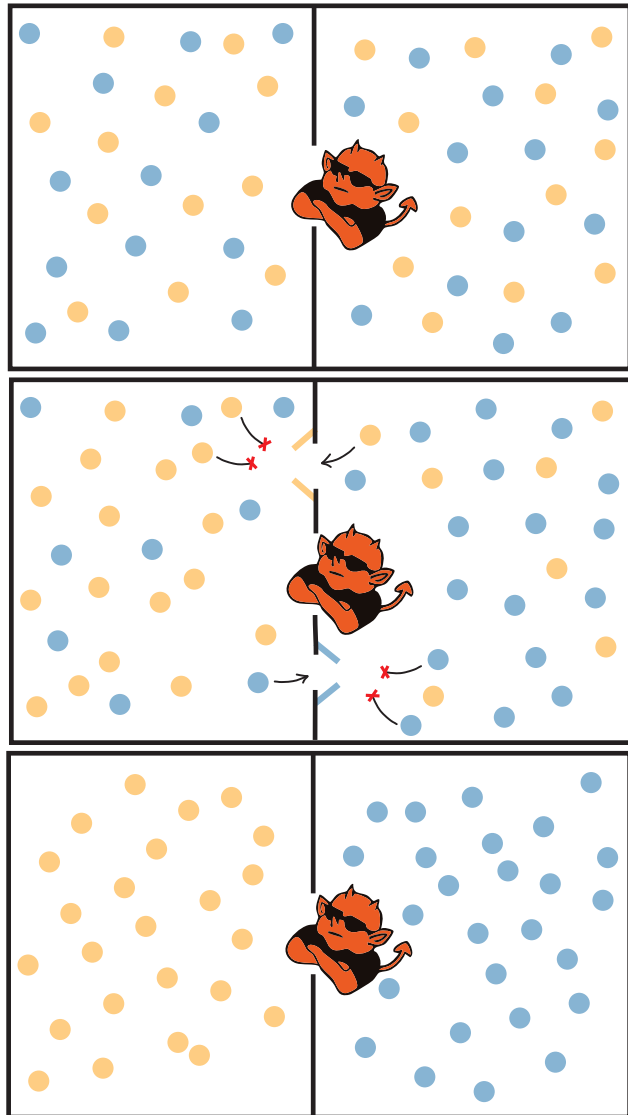
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**The Demon is  
in the Details**

**Top (Maxwell's Demon):** The classic Maxwell's Demon thought experiment. A demon monitors molecules in a gas and selectively opens a door to let fast-moving (hot) molecules through in one direction and slow-moving (cold) molecules through the other. Over time, this creates a temperature gradient without performing mechanical work, seemingly violating the second law of thermodynamics.

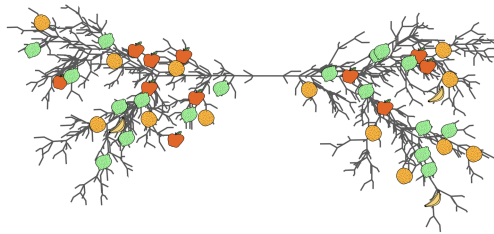
**Bottom Left (Work Cost):** First resolution—work-based measurement cost (Szilard 1929, Brillouin 1951). Determining each molecule's speed and deciding whether to open the door requires physical measurement processes that generate entropy or consume work, preventing a net decrease in total entropy.

**Bottom Right (Memory Erasure):** Second resolution—memory erasure cost (Landauer 1961, Bennett 1982). Even if measurement and control were performed reversibly with no work cost, the demon's finite memory would eventually fill. Erasing past measurement records to store new data increases entropy by at least  $k \ln 2$  per bit erased (Landauer's Principle), ensuring the second law remains intact. Either way, the apparent paradox dissolves when information-processing steps are properly accounted for.



# The Demon is in the Details

Maxwell's Demon, proposed in 1867, describes a thought experiment where a tiny being controls a door between two gas chambers, selectively allowing fast molecules into one chamber and slow ones into another. This sorting creates a temperature gradient from uniformity, seemingly decreasing entropy and violating the second law of thermodynamics. The resolutions are through work costs of measurement and the information-theoretic cost of manipulating information.



MAXWELL'S DEMON ◦ SECOND LAW CHALLENGE ◦ ENTROPY &  
INFORMATION ◦ BOLZMANN STATISTICS ◦ MOLECULAR  
SORTING ◦ LANDAUER'S PRINCIPLE ◦ BENNETT'S  
RESOLUTION ◦ INFORMATION ERASURE  
COST ◦ THERMODYNAMIC COMPUTING ◦ INFORMATION IS  
PHYSICAL ◦ MEMORY CYCLE LIMITS

*« Seul un être aux sens infiniment subtils,  
tel que le démon de Maxwell,  
pourrait démêler cet écheveau embrouillé  
et remonter le cours de l'univers. »*

(“Only a being with infinitely subtle senses, such as Maxwell's demon, could unravel this tangled skein and reverse the course of the universe.”)

— Poincaré, 1902

“Oh, ye seekers after perpetual motion,  
how many vain chimeras have you pursued?  
Go and take your place with the alchemists!”

— Da Vinci, 1500s

## The Demon is in the Details

The roots of thermodynamics trace back to early nineteenth-century efforts to understand the efficiency of heat engines. In the 1820s, Sadi Carnot introduced the idea of reversible cycles and the notion that heat could be partially transformed into work, bounded by what would later be called the second law of thermodynamics. His work, though framed in a caloric theory, anticipated a fundamental limitation: that no engine could be more efficient than a reversible one operating between two heat reservoirs.

Building on this foundation, Rudolf Clausius in 1865 formally introduced and named the concept of entropy, giving the second law a precise mathematical expression: in any real process, the total entropy of an isolated system tends to increase. Earlier, in 1851, William Thomson (Lord Kelvin) offered an alternative formulation, asserting the impossibility of converting all heat from a single reservoir into work without other effects—essentially forbidding perpetual motion machines of the second kind.

While these formulations were macroscopic and phenomenological, physicists such as Ludwig Boltzmann sought to derive them from microscopic principles, modelling gases as vast ensembles of molecules obeying Newtonian mechanics. This kinetic theory offered statistical interpretations of thermodynamic quantities, suggesting that entropy increase reflected the overwhelmingly probable behaviour of particle ensembles rather than an inviolable mechanical law.

It was in this context—where thermodynamics was seen as emergent from statistical regularities, yet grounded in reversible microscopic dynamics—that James Clerk Maxwell introduced his thought experiment in 1867. He aimed to probe the assumptions underlying the second law by imagining an idealised being capable of intervening at the molecular level, potentially subverting the macroscopic flow of entropy without violating any mechanical law.

Thermal systems are characterised by macroscopic quantities—temperature, pressure, and volume—that arise from the statistical behaviour of countless microscopic constituents. Each molecule in a gas possesses position and velocity at every instant. Macroscopic observables summarise the collective dynamics of trillions of particles.

A single macroscopic state corresponds to countless microscopic configurations. The same pressure and temperature can arise from different combinations of molecular positions and velocities. This multiplicity is central to statistical mechanics, where macroscopic descriptions average over the microstates that realise them.

Entropy quantifies the logarithm of the number of microstates compatible with a given macrostate. In the Boltzmann formulation, the entropy (Boltzmann, 1877)  $S$  of a system is expressed as  $S = k_B \ln \Omega$ , where  $k_B$  is Boltzmann's constant and  $\Omega$  denotes the number of microstates. This mathematical framework captures both the multiplicity of configurations and the incompleteness of macroscopic information.

The Boltzmann constant  $k_B = 1.380649 \times 10^{-23}$  J/K (exact, SI) bridges microscopic and macroscopic worlds. It converts between energy scales of individual particles (joules)

and thermal energy (kelvins). At room temperature ( $T \approx 300$  K), the thermal energy  $k_B T \approx 4.14 \times 10^{-21}$  J sets the scale for molecular motion and thermal fluctuations.

The second law of thermodynamics asserts that in an isolated system, entropy cannot decrease. Natural processes tend toward macrostates with greater multiplicity because they are overwhelmingly more probable—there are more ways to achieve a general, high-entropy macrostate than to achieve a lower-entropy, specific macrostate, so any ‘random’ process will tend to increase entropy. The law governs irreversibility in macroscopic phenomena and forbids spontaneous reorganisation into low-entropy configurations. Though microscopic dynamics allow rare fluctuations, most accessible microstates correspond to thermal equilibrium.

The second law admits equivalent formulations: Clausius forbids spontaneous heat flow from cold to hot; Kelvin rules out complete conversion of heat to work in cyclic processes. Both capture energy’s unidirectional dispersal.

While microscopic laws (Newtonian mechanics, Schrödinger equation) are time-reversal invariant, macroscopic irreversibility emerges from statistical asymmetry. Individual molecular collisions remain reversible, but aggregate behaviour favours higher-entropy macrostates due to their numerical dominance.

Although the total phase space volume occupied by a system is conserved under Hamiltonian evolution, as guaranteed by Liouville’s theorem, entropy can increase. Fine-grained distributions evolve into intricate structures that, when viewed with any coarse-graining appropriate to macroscopic observations, appear more uniform, corresponding to higher entropy.

Temperature reflects the average kinetic energy per degree of freedom in a system. In classical gases, the distribution of particle energies follows the Maxwell–Boltzmann distribution, while in more general statistical ensembles, the Boltzmann distribution governs the probability of finding the system in a given microstate, establishing a link between microscopic motion and macroscopic thermodynamic parameters.

Thermodynamic processes exchange energy through work and heat. Entropy tracks irreversible energy dispersal and loss of microscopic information. Work represents organised energy transfer; heat denotes disorganised exchange. The second law ensures some energy becomes unavailable for work.

The second law introduces the thermodynamic arrow of time. This arrow derives not from time-symmetric laws of motion, but from statistical tendencies toward higher entropy. Systems evolve from ordered to disordered states, establishing asymmetry between past and future.

Entropy represents the missing information about the system’s precise microstate. In this view, thermodynamic entropy parallels concepts from information theory, linking the physical evolution of systems with the informational limitations inherent in macroscopic descriptions.

In 1867, James Clerk Maxwell introduced a thought experiment that challenged the apparent absoluteness of the second law of thermodynamics. He imagined a sealed box filled with

gas at thermal equilibrium, where molecules moved randomly at a range of speeds and directions. A partition divided the box into two chambers, A and B, with a small frictionless door controlled by a hypothetical observer: the demon.

The demon monitors molecules approaching the door without mechanical work or external energy. Fast molecules from A pass to B; slow molecules from B pass to A. Others are blocked. Faster molecules accumulate in B, slower ones in A.

This sorting creates a temperature gradient. Heat flows from cold to hot without external energy, contradicting Clausius's formulation. Entropy decreases: the uniform configuration becomes ordered by temperature difference.

The paradox: without work or external energy, the system evolves toward lower entropy. The demon appears to circumvent thermodynamic constraints.

Two approaches resolve this paradox:

**The Work-Based Approach** argues that the demon cannot operate without performing thermodynamic work. To distinguish between fast and slow molecules, the demon must interact with them, perhaps by shining light to measure their velocities or by mechanically probing their kinetic energies. These measurement processes necessarily require energy input and generate entropy. However, this approach faces a limitation: it cannot establish a precise quantitative relationship between the work invested in measurement and the entropy reduction achieved through sorting. The energy costs of individual molecular measurements depend on the specific measurement apparatus and protocols, making it difficult to prove that the entropy increase from measurement operations exactly compensates for the entropy decrease from molecular sorting.

**The Information-Erasure Approach** offers a more satisfactory resolution by focusing not on measurement costs, but on the logical requirements of cyclic operation. This approach, developed by Rolf Landauer and Charles Bennett, recognises that for the demon to operate cyclically, it must eventually erase the information stored in its memory. Landauer's principle establishes that erasing one bit of information (Landauer, 1961) requires a minimum energy dissipation of  $k_B T \ln 2$ , where  $k_B$  is Boltzmann's constant and  $T$  the temperature of the environment. This energy cost is independent of the physical implementation—it represents a thermodynamic limit on information processing.

Bennett's insight was that this erasure cost provides exact entropy accounting. In each cycle, the demon reduces the gas entropy by  $k_B \ln 2$  (corresponding to one bit of information about molecular positions). To continue operating, the demon must erase one bit from its memory, which necessarily increases the environment's entropy by at least  $k_B \ln 2$ . The entropy reduction from molecular sorting is precisely compensated by the entropy increase from information erasure. No net entropy decrease occurs when all components, gas, demon memory, and thermal environment, are included in the accounting.

This information-theoretic resolution is remarkable because it establishes that **information is physical**. The demon's memory, though conceptually abstract, must be realised in some material substrate subject to thermodynamic laws. The act of erasing information is not merely a computational operation but a physical process that generates heat and increases entropy.

The information-erasure approach also reveals why attempts to circumvent the erasure requirement fail. If the demon preserves information indefinitely to avoid erasure costs, its memory eventually becomes full, preventing further operation. If the demon attempts to reset its memory without erasure, perhaps through reversible computation, the information is merely transferred elsewhere in the system, requiring eventual erasure at some location. The second law cannot be circumvented by clever information management; it emerges inevitably from the statistical nature of many-body systems and the physical reality of information storage.

The ‘piston-demon’ model suggests the moving partition itself serves as memory, its position encoding molecular information. The resolution depends on system boundaries and whether demon-plus-gas constitutes a closed system.

Quantum mechanics adds complexities: measurement disturbs systems, and indistinguishability constrains sorting. Quantum Maxwell’s demons demonstrate how coherence and decoherence affect entropy accounting, probing connections between information, measurement, and thermodynamics.

### *Does a Full Hard Drive Weigh More?*

If information is physical, does a full hard drive weigh more than an empty one? Some theoretical arguments suggest tiny differences, though not in any measurable way.

**Information Entropy:** A terabyte ( $8 \times 10^{12}$  bits) of random data carries maximal Shannon entropy. Erasing that data would, by Landauer’s principle, dissipate at least  $E = Nk_B T \ln 2 \approx 2.3 \times 10^{-8}$  J at room temperature, equivalent to  $\Delta m = E/c^2 \approx 2.6 \times 10^{-22}$  g. This represents heat released during erasure, not extra energy stored in the drive—no more than a (6, 6) dice throw weighs more than (1, 4).

**Solid-State Drives:** In flash memory, a ‘1’ corresponds to additional trapped electrons in a floating gate. A terabyte written entirely with ‘1’ bits contains roughly  $10^{16}$  extra electrons, adding about  $10^{-11}$  g. This effect is real but fifteen orders of magnitude smaller than the drive’s total mass and far beyond detectability.

## Exercises

### Energy Conservation to Solve Complex Problems

In classical mechanics, many systems that appear to require force analysis, Newton's laws, or torque computations can be solved using the principle of energy conservation. The following problems invite you to discover how straightforward solutions can emerge when the total mechanical energy is conserved.

#### 1. Rolling Sphere on an Incline

A solid sphere of mass  $m$  and radius  $R$  is placed at the top of a frictional incline of angle  $\theta$  and allowed to roll down without slipping. Using energy conservation (not Newton's laws), determine the acceleration of the sphere's centre of mass.

*Hint:* Total mechanical energy includes both translational and rotational kinetic energies.

#### 2. Yo-Yo Drop

A yo-yo of mass  $m$  is held so that its string is taut and then released. The string unwinds without slipping as the yo-yo descends. The axle radius is  $r$  and the moment of inertia about the centre is  $I$ . Use energy conservation to determine the downward acceleration of the yo-yo's centre of mass.

*Hint:* The yo-yo's kinetic energy has both linear and rotational components; relate the angular speed to the linear speed via the axle radius.

#### 3. Chain Falling Off a Table

A uniform chain of linear mass density  $\lambda$  lies coiled on a horizontal frictionless table. At time  $t = 0$ , a small length starts to hang off the edge and the chain begins to slide off under gravity. Assuming no friction and no energy loss, use conservation of mechanical energy to find the acceleration of the chain as it falls.

*Hint:* The centre of mass of the hanging portion descends while its kinetic energy increases.

#### 4. Man Walking on a Boat

A man of mass  $m$  walks a distance  $d$  from one end of a boat of mass  $M$  to the other. The boat floats on frictionless water. Determine how far and in what direction the boat moves relative to the water while the man walks. Use momentum conservation—no external horizontal forces act on the system.

*Hint:* The centre of mass of the system must remain fixed in the horizontal direction.

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**Answers:** 1:  $a = \frac{5}{7}g \sin \theta$  2:  $a = \frac{mg}{m + \frac{2}{I}r^2}$  3:  $a = \frac{2}{g}$  4: Boat disp. =  $-\frac{m}{m+M}d$

## Thermodynamic Accounting in the Classical Szilard Engine

### Introduction

The Szilard engine models a single classical particle confined in a box connected to a thermal reservoir at temperature  $T$ . A partition is inserted, the particle is measured, and expansion performs work. The demon, modelled as a finite memory device, must be reset for reuse. This section formally evaluates the extracted work and the entropy budget, showing that total entropy remains non-decreasing when all components are included.

### Work from Isothermal Expansion

After measurement, the particle occupies volume  $V/2$ . Isothermal expansion to volume  $V$  yields mechanical work:

$$W_{\text{ext}} = \int_{V/2}^V \frac{k_B T}{V'} dV' = k_B T \ln 2.$$

Let  $\sigma \equiv k_B \ln 2$ . Then:

$$W_{\text{ext}} = T\sigma \quad \text{and} \quad \Delta S_{\text{gas}} = \sigma.$$

This reflects the entropy gained by the gas during expansion under constant temperature, which accounts for the increase in accessible microstates as the volume doubles.

### Memory Reset and Landauer Bound

To begin a new cycle, the demon must erase one bit of information. Erasure is a logically irreversible operation mapping two equiprobable states to one. According to Landauer's principle, the minimum heat dissipated into the reservoir is:

$$Q_{\text{erase}} \geq T\sigma \quad , \quad \Delta S_{\text{mem}} = -\sigma, \quad \Delta S_{\text{env}} \geq \sigma.$$

This entropy increase in the environment offsets the decrease in the demon's memory. Even in an idealised quasistatic erasure process, the bound cannot be avoided.

### Entropy Ledger Over a Full Cycle

We now compute entropy changes for all subsystems. Let  $G$  be the gas,  $M$  the memory, and  $E$  the thermal environment. Then:

$$\Delta S_G = -\sigma \quad (\text{localization dur. measur.})$$

$$\Delta S_G = +\sigma \quad (\text{isothermal expansion})$$

$$\Rightarrow \Delta S_G = 0$$

$$\Delta S_M = +\sigma \quad (\text{information recorded})$$

$$\Delta S_M = -\sigma \quad (\text{memory erased})$$

$$\Rightarrow \Delta S_M = 0$$

$$\Delta S_E = -\sigma \quad (\text{heat drawn dur. expansion})$$

$$\Delta S_E \geq +\sigma \quad (\text{heat dumped dur. erasure})$$

$$\Rightarrow \Delta S_E \geq 0.$$

Summing over all contributions:

$$\Delta S_{\text{total}} = \Delta S_G + \Delta S_M + \Delta S_E \geq 0.$$

The equality holds in the quasistatic limit where each step is ideal and reversible. Any deviation—e.g., finite-time processes or imperfect measurement—adds entropy.

### Conclusion

The apparent entropy reduction induced by the demon is exactly counterbalanced by the entropy cost of erasing its memory. Though the demon performs no mechanical work, its function relies on acquiring and discarding information—a process embedded in physical degrees of freedom. When all elements are included in the thermodynamic ledger, the second law remains intact. No net entropy decrease occurs, and no violation arises.

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